Low power High performance adder with Prefix Tree Structure configuration

Venkata K. Ramanaiah
Associate Professor, Dept. of ECE, YSR Engineering College of Yogi Vemana University, Proddatur, Andhra Pradesh, India

ABSTRACT: In the advancements of modern technology the field of nanometer technology makes to maximize the speed performance and minimize the power of logic designs particularly in the binary arithmetic digital design stream. This can be achieved by Parallel Prefix Tree Structure. Proposed design investigates a 64-bit hybrid digital adder circuit by using radix-4 tree structure and carry select adder. As the design is imposed with carry select, the carry propagation time is reduced. The proposed design have designed and simulated using verilog hardware description language (HDL) using Xilinx Integrated Software Environment (ISE) 14.3 Design Suite. These designs are implemented in Xilinx Field Programmable Gate Arrays. The experimental results proved that the proposed 64-bit hybrid adder is superior to other adders, and has 2.71ns delay time, 9.58 mw average power.

KEYWORDS: Carry select adder, FPGA, hybrid adder, low power, parallel prefix adder

I. INTRODUCTION

The binary addition is the basic arithmetic operation in any digital circuit and it becomes essential in most of the digital systems including arithmetic and logic unit (ALU), microprocessors, digital signal processing (DSP) and floating point unit (FPU). With the rapid growth in portable electronic equipments and mobile communication devices, demand to low voltage and low power technology for VLSI applications is great increasing. In general, high speed adder includes carry look ahead adder (CLA), carry select adder (CSA), carry bypass adder (CBA), conditional sum adder and later developed parallel prefix adder (PPA). Different prefix algorithms and tree topologies (BKA, STA, KSA, SKA) of PPAs have been implemented for solving delay, area, and power efficiencies. Design of an appropriate tree topology is a trade-off among the fan-out, the wiring count and the logic level [1]. Recently, several high-performance 64-bit adders have been reported in [2-3]. The high-speed 64-bit adder [2] is hybrid sparse radix-4 prefix tree and CSA based on energy-delay optimization methodology. In this paper, a 64-bit hybrid adder is proposed to combine both prefix tree structure (PTS) and CSA for fetching low voltage and low power features. The three stages prefix tree of the 64-bit hybrid adder computes carries, and then the CSA with add-one circuit selects sums by these carries. Otherwise, the CBA has been added at the third stage of the PTS to diminish fan-ins, fan-outs, wiring counts and transistor counts. With respect to low voltage low power method, complementary metal oxide semiconductor (CMOS) logic, transmission gate (TG) logic, and pass transistor logic (PTL) are applied in proposed design to fetch full swing operation at each node.

II. EXISTING SYSTEM

In fig.1, it is a 4 bit ripple carry adder having a first sum bit should wait and depend until input carry is given, the second sum bit should wait and depend until previous carry is propagated and so on. Finally the output sum should wait until all previous carries are generated and propagated will take more time, will results in large delay. To overcome this type of problems the carry prediction circuits can be designed, and described as follows.

![Fig.1: Four bit ripple carry adder](image-url)
In order to reduce the delay in RCA (or) to propagate the carry in advance, we go for carry look ahead adder. Basically this adder works on two operations called propagate and generate. The propagate and generate equations are given by:

\[ P_i = A_i \oplus B_i \]  

\[ G_i = A_i \cdot B_i \]  

For 4 bit CLA, the propagated carry equations are given as

\[ C_1 = G_0 + P_0 \cdot C_0 \]  

\[ C_2 = G_1 + P_1 \cdot G_0 + P_1 \cdot P_0 \cdot C_0 \]  

\[ C_3 = G_2 + P_2 \cdot G_1 + P_2 \cdot P_1 \cdot G_0 + P_2 \cdot P_1 \cdot P_0 \cdot C_0 \]  

\[ C_4 = G_3 + P_3 \cdot G_2 + P_3 \cdot P_2 \cdot G_1 + P_3 \cdot P_2 \cdot P_1 \cdot G_0 + P_3 \cdot P_2 \cdot P_1 \cdot P_0 \cdot C_0 \]  

Equations (3), (4), (5) and (6) are observed that, the carry complexity increases by increasing the adder bit width. So designing higher bit CLA becomes complexity. In this way, for the higher bit of CLA’s, the carry complexity increases by increasing the width of the adder. So results in bounded fan-in rather than unbounded fan-in, when designing wide width adders. In order to compute the carries in advance without delay and complexity, there is a concept called Parallel prefix approach.

The PPA’s pre-computes generate and propagate signals are presented in [4]. Using the fundamental carry operator, these computed signals are combined in [5]. The fundamental carry operator is denoted by the symbol “\( \circ \)”,

\[ (g_L, p_L) \circ (g_R, p_R) = (g_L + p_L \cdot g_R, p_L, p_R) \]  

For example, 4 bit CLA carry equation is given by,

\[ C_4 = (g_4, p_4) \circ [(g_3, p_3) \circ [(g_4, p_4) \circ (g_3, p_3)]] \]  

For example, 4 bit PPA carry equation is given by,

\[ C_4 = [(g_4, p_4) \circ (g_3, p_3)] \circ [(g_4, p_4) \circ (g_3, p_3)] \]  

From equations (8) and (9) it is clear that, the CLA takes three steps to generate the carry, but PPA takes two steps to generate the carry.
PPA’s basically consists of three stages during addition process. They are

1. Pre computation
2. Prefix stage
3. Final computation, the structure of PPA is shown in fig.2

Fig.3: Black and Gray cells

Fig.4: 16-bit Sparse KoggeStone adder
Figure 3 shows the definitions of cells that are used in prefix structures, including BC and GC. For analysis of various parallel prefix structures, see [4], [5] & [6].

**Kogge Stone Adder (KSA)**

KSA is another of prefix trees that use the fewest logic levels. A 16-bit KSA is shown in Figure 6. The 16 bit kogge stone adder uses BC’s and GC’s and it won’t use full adders. The 16 bit KSA uses 36 BC’s and 15 GC’s. And this adder totally operates on generate and propagate blocks. So the delay is less when compared to the previous SKA and STA. The 16 bit KSA is shown in figure 4. In this KSA, there are no full adder blocks like SKA and STA [7] & [8].

### III. PROPOSED 64-BIT HYBRID ARCHITECTURE

The figure 5 shows new hybrid adder, is constructed with three modules, which consists of Generate or Propagate Generation (GPG), Prefix Tree Structure (PTS) and the CSA with add-one circuit. The initial stage or starting stage of the GPG generates individual generate and propagate signals for each bit position. The middle stage of the PTS computes some specific carries to the next stage for the CSA. The final stage of the CSA with add-one circuit selects the proper sum as the output. It is advantages that the initial stage of sharing generates and propagates signals in both PTS and CSA blocks to reduce the hardware structure overheads to achieve more compact area with less leakage power.

![Fig.5: Block diagram of proposed hybrid architecture](image)

In PPA, the carry computation approach dominates the overall performance of the adder design. In order to fetch faster computation, lot of parallel prefix tree structure topologies have been designed and developed to have a good trade-offs between speed, power and area. The more efficient way is implementing parallelizable prefix computation by taking advantage of the associative operator “o” [9], [0].

The generate (g) and propagate (p) signals can be defined as follow:

\[(g, p) \circ (g', p') = (g + pg', pp')\]  \hspace{1cm} (10)

Giving a series of bits i…j…k, the group generate/propagate pair \((g_{i:k} , p_{i:k})\) can be expressed in terms of input signals \(p_j\) and \(g_j\) from bit position \(i\) to \(k\), respectively. Therefore,

\[(g_{i:k} , p_{i:k}) = (g_i , p_i) \circ (g_{i+1} , p_{i+1}) \circ (g_{i+1} , p_{i+1}) \circ (g_{i-1} , p_{i-1}) \circ ... \circ (g_k , p_k)\]  \hspace{1cm} (11)
The invented 64 bit hybrid adder has been designed based on PTS and CSA, as shown in Figure 6. For a group of four bits, the radix-4, 64-bit hybrid adder is composed of three stages. According to the relationship between stage and radix in a prefix tree [2],[11],[12] the fewer stages depend on higher radix adopted, and the least stages are applied in prefix adder results in the potential higher speed and lowest power consumption. A 4-bit CSA is taken in my consideration is due to the delay time of a 4-bit carry ripple adder (CRA) module is slightly less than that of PTS. Consequently, every four-bit of PTS computes a carry for Corresponding 4-bit CSA module. To achieve the goal of high speed adder, carry-in signal (cin) directly connects to the second stage. The proposed structure differs greatly from other architectures in which carry-in signal are linked to the first stage. In such scheme, the critical path of proposed design has reduced load capacitance. As a result, the total performance of the adder will be boosted.

In the proposed 64-bit hybrid adder, the generate signal (gi) and propagate signal (pi) are generated at the initial stage. The radix-4 PTS, the middle stage, computes carries to the CSA modules in final stage. For the first and second stages, every module utilizes CMOS logic to complete the intermediate carry. To diminish the fan-out at the second stage as the fan-in at the third stage, CBA is adopted at the third stage for terminal carry output. This turns out to greatly reduce the wiring counts, so the third stage owns compact area and lower power consumption. And CBAs skip over long carry ripple to reduce the delay time with fewer transistor numbers. At the final stage, the 4-bit CSA quickly produce sums through MUXs when carry signal arrived. Fig. 7 shows the simulated waveforms, and table 1 gives comparison of various adders.

V. RESULT AND DISCUSSION

Fig. 7: Wave forms
Table 1. Comparison of adders

<table>
<thead>
<tr>
<th>Adder Name (16bit)</th>
<th>Total Delay (ns) in Xilinx ISE 14.3</th>
<th>Power (mW) Xilinx ISE 14.3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sparse Kogge Stone</td>
<td>4.46</td>
<td>42.38</td>
</tr>
<tr>
<td>Spanning Tree</td>
<td>3.98</td>
<td>42.38</td>
</tr>
<tr>
<td>Kogge Stone</td>
<td>4.53</td>
<td>42.38</td>
</tr>
<tr>
<td>Brent Kung</td>
<td>4.12</td>
<td>42.38</td>
</tr>
<tr>
<td>Proposed (64bit) adder</td>
<td>2.71</td>
<td>9.58</td>
</tr>
</tbody>
</table>

VI. CONCLUSION

The proposed hybrid adder is composed of the radix-4 prefix tree structure and the CSA to benefit the high speed. The experimental results show that the proposed 64-bit hybrid adder has 2.71ns delay, consumes 9.58mw power and utilization of lower look at tables (LUTs). As results, the design achieves superior power, speed, and area constraints and therefore this adder efficient and plays a crucial role in Processors, and arithmetic and logic operations etc., compared with other existing designs.

REFERENCES