



# Diagnosis of the Best Method for Wind Speed Extrapolation

Dr. Firas A. Hadi

Department of Wind Energy, Ministry of Science and Technology, Baghdad, Iraq

**ABSTRACT:** The standard height of meteorological towers for wind speed observations is 10 meters. Since wind turbine hub heights are typically more than this height, extrapolation of wind speeds to the planned hub height is usually required, the most elementary models for predicting the adjusted wind speed are power law and logarithmic law. The purpose of this paper is to extrapolate the wind speed and power density to different heights using power law, logarithmic law, and wind speed distribution extrapolation; then the results were compared with the real data taken from sensors located at different heights for the purpose of knowing the best representation method. The sensors are installed at 10, 30, 52 meters heights from ground surface at Al-Shehabi site in Iraq. Also, for more benefits, both of results and the observed data (real data) were compared with wind resource map of Iraq (Geosun) in order to know the accuracy of map's data. It is found that the wind speed distribution extrapolation gives more acceptable results than the power and logarithmic laws for extrapolation procedure, at the same time it was proved that how much extent the validity of map is.

**KEYWORDS:** Extrapolation, Power law, Log law, Distribution Extrapolation.

Nomenclature	
<b>Abbreviations</b>	
WT	wind turbine
PL	power law
LogL	logarithmic law
LIDAR	light detection and ranging
SODAR	Sonic detection and ranging
<b>Variables</b>	
$v_1$	wind speed at reference height (m/sec)
$v_2$	wind speed at another height (m/sec)
$z_0$	roughness length (m)
$z_1$	roughness length at reference height
$z_2$	roughness length at another height
	$\rho$ density of the air
	$Z_{o1}$ is roughness length at reference location
	$Z_{o2}$ is roughness length at destination location
	$n$ Weibull distribution extrapolation exponent
	$\alpha$ or Alpha Hellman's wind shear exponent
	$z$ elevation above the ground
	$k_{von}$ Karman constant
	$u_*$ friction velocity
	$\tau$ surface value of the shear
	$h_1$ wind speed at a reference height
	$h_2$ wind speed at another height (hub height)
	$c_1$ Weibull scale factor at $h_1$ height
	$k_1$ Weibull shape factor at $h_1$ height
	$c_2$ Weibull scale factor at $h_2$ height
	$k_2$ Weibull scale factor at $h_2$ height

## I. INTRODUCTION

Wind measurements are generally performed below WT hub heights owing to the higher measurement and tower cost. Therefore, a wind shear model proves to be necessary to extrapolate the observed wind resource from the available lower heights to the wind turbine hub height, [1].

Wind speed profile is affected by the roughness of the landscape, which is measured by the surface roughness length. A high roughness tends to decrease wind speed and cause the wind to slow down near the ground, or vice versa, the wind speed increases with height increases. The rate of wind speed increases according to the height and roughness of the terrain. In particular, wind shear is strongly affected by atmospheric stratification, varying by hour of day, month/season

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of year, and from one year to the other. Thus, wind speed extrapolation might be regarded as one of the most critical uncertainty factor affecting wind power assessment, particularly when considering the increasing size of modern wind turbines. Actually, critical errors between estimated and actual energy output may result from application of this extrapolation, and the use of devices such as LIDAR or SODAR to eliminate errors due to shear model uncertainty largely increase the costs of a wind power project, often making it economically not viable, while increasing knowledge on wind shear models to strengthen their reliability appears as preferable, [1].

In this study a validity of each power law, logarithmic law, speed distribution, and Geosun map is achieved after a comparison with the real data, this will show us the most applicable one at Al-Shehabi site.

## AREA OF STUDY

The feasibility and applicability of wind energy development depends on the physical characteristics of the study area and the wind resource. The region is located in the area between Maysan and Wasit. It is 112 km from Maysan, 85 km from Wasit, and about 220 km from Baghdad at position 32.77°N 46.70°E; Figure. 1 shows the location of chosen site in eastern region near the border between Iraq and Iran.



Fig. 1 Iraq satellite image to indicate the area of study

## II. BACKGROUND

Since methods and models applied in the current work are the same as in the previous one, the reader should refer to the corresponding Background section [2], where the following are presented: (i) the PL by Hellman derived equation to calculate alpha base on record so  $v_1$  and  $v_2$ ; (ii) the Log L, and derived equation to assess  $z_0$  under neutral stability conditions; (iii) models for estimating alpha such as Smedman, Höglström and Höglström [3], and (iv) models for estimating alpha such as Justus and Mikhail [4].

## III. GEOSUN MAP

Geosun map is wind resource map or wind energy map of Iraq at 3 heights above ground at high resolution (1 km x 1 km). The wind map is generated with the atmospheric Mesoscale model SKIRON and presented in Geographic Information System (GIS) format. This map has



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Wind View allows users to view and query wind data in an interactive environment, as well as modifies, copy, and print maps. With the selected methodology it is possible to obtain virtual hourly datasets at any specified position and any height above ground level.

## IV. LOGARITHMIC LAW

The logarithmic law origins lie in the boundary layer fluid mechanics and atmospheric research. To determine the horizontal velocity ( $v$ ) at a height ( $z$ ), it is commonly expressed as follows:

$$v(z) = \left(\frac{u_*}{\kappa}\right) \ln\left(\frac{z}{z_0}\right) \quad (1)$$

Where  $\kappa = 0.4$  is von Karman constant. ( $u_* = \left(\frac{\tau}{\rho}\right)^{1/2}$ ). The roughness length ( $z_0$ ) describes the roughness of the ground or terrain where the wind is blowing. There are cases where wind velocity  $v_1$  is known and required at another height ( $z_2$ ) in a case that can be derived from Eq.1 [5]:

$$v_2 = v_1 \frac{\ln(z_2) - \ln(z_0)}{\ln(z_1) - \ln(z_0)} \quad (2)$$

It is a simple expression to solve, as it eliminates the need to calculate the friction velocity and von Karman constant, which could be difficult to estimate in the atmosphere. A neutral wind profile is assumed, where convection is negligible, the lapse rate (the fall of temperature in the troposphere with height) is nearly adiabatic.

Note that Eq.2 gives estimation on the speed at one location. In case one wants to compare two locations (for example, meteorological station and wind turbine site), each with its own roughness length with similar wind profile, then Wieringa's assumption that the wind speed at 60m height is unaffected by the roughness, leads to the formula, [6]:

$$\frac{v_2(z_2)}{v_1(z_1)} = \left[ \frac{\ln\left(\frac{60}{z_1}\right) \ln(z_2/z_2)}{\ln\left(\frac{60}{z_2}\right) \ln(z_1/z_1)} \right] \quad (3)$$

## V. POWER LAW

The power law equation is a simple, yet useful model of the vertical wind profile which was first proposed by Hellman (1916). The power law profile assumes that the ratio of wind speeds at different heights can be found by the following equation:

$$v_2 = v_1 \left(\frac{h_2}{h_1}\right)^\alpha \quad (4)$$

The shear exponent  $\alpha$  (Alpha) can be directly measured once records of  $v_1$  and  $v_2$  are available:

$$\alpha = \frac{\ln(v_2/v_1)}{\ln(h_2/h_1)} \quad (5)$$

The shape of the power law profile is determined by ( $\alpha$ ), and the shape of the LogL profile is determined by the roughness length ( $z_0$ ). Figure (2) depicts both types of profiles [Basim].

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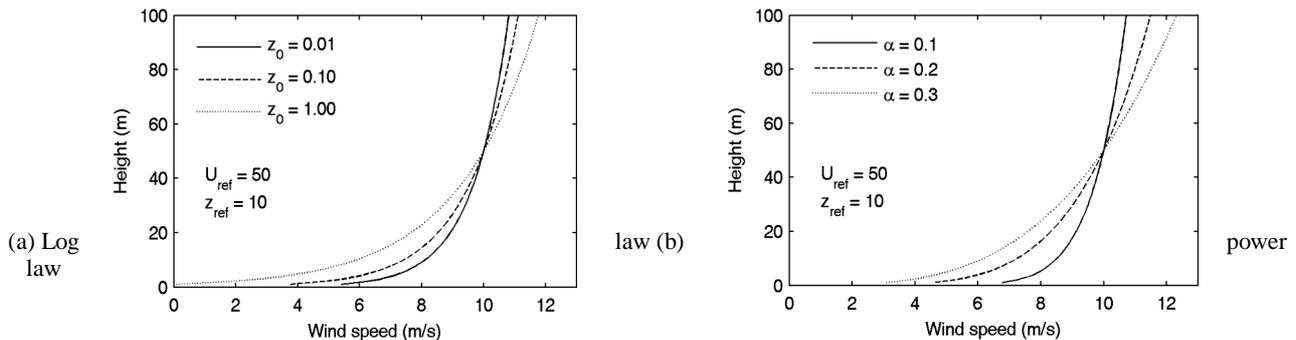


Fig.2 Example wind shear profiles using Log law and power law models

If the wind shear coefficient,  $\alpha$ , cannot be determined correctly, the difference between the predicted and observed wind energy production might be up to 40%, due to turbulence effects, time interval of wind data measurement, and the extrapolation of the data from reference height to hub heights. In the literature, the wind shear coefficient is a highly variable quantity, often changing from less than 0.14 during the day to more than 0.5 at night over the same terrain. Also, wind shear coefficient was measured to typically range from 0.40 in urban areas with high buildings to 0.10 over smooth, hard ground, lakes or ocean. However, in real situations, a wind shear coefficient is not constant and depends on numerous factors, including atmospheric conditions, temperature, pressure, humidity, time of day, seasons of the year, the mean wind speed, direction, and nature of terrain. Table 1 demonstrates the various wind shear coefficients for different type of topography and geography, [1].

Table 1: Shear exponent values according to different Terrain Type

Terrain Type	value
Lake, ocean, and smooth hard ground	0.1
Foot-high grass on level ground	0.15
Tall crops, hedges, and shrubs	0.2
Wooded country with many trees	0.25
Small town with some trees and shrubs	0.3
City area with tall buildings	0.4

From Eq. (4),  $\alpha$  can be directly measured once records of  $v_1$  and  $v_2$  are available:

## VI. THE WEIBULL WIND SPEED DISTRIBUTION EXTRAPOLATION

Justus and Mikhail suggested a useful full range of wind speed, as required to specify the wind speed probability distribution. They demonstrated the power law relationship between wind profiles Eq. 4 to be consistent with the height variation of the Weibull wind speed distribution, at least under the assumption of heights below 100m and a fairly level terrain (though over a wide range of roughness length) [8]. Thus, if Weibull probability distribution at reference height  $h_1$  is  $p(v_1)$ , then  $p(v_2)$  at any other height  $h_2$  may be derived. In other words, if  $c_1$  and  $k_1$  Weibull functions are known at. Some anemometer height  $h_1$ , then the values of  $c_2$  and  $k_2$  at any desired height  $h_2$  (e.g., the turbine hub height) can be assessed by:

$$c_2 = c_1 \left( \frac{h_2}{h_1} \right)^n \quad (6)$$

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$$k_2 = k_1 \frac{1 - 0.0881 \ln(h_1/h_r)}{1 - 0.0881 \ln(h_2/h_r)} \quad (7)$$

Where  $h_r$ , a reference height of 10m and the exponent  $n$  is was empirically found to be:

$$n = \frac{0.37 - 0.0881 \ln(c_1)}{1 - 0.0881 \ln(h_1/h_r)} \quad (8)$$

Note that for  $n$  a different notation from a commonly used to emphasize its different meaning, although the  $\alpha$  and  $n$  strict relationship has been experimentally demonstrated by [9]. He also pointed out that, while  $\alpha$  depends on several surface properties,  $n$  only depends on  $c$  and  $h$  of the measurement height.

## VII. RESULTS AND DISCUSSIONS

The histograms for Al-Shehabi site at 10m and 52m heights are shown in Fig.3 below, where most of the wind speeds are concentrated under 5m/sec from the distribution (Fig.3-a), such that 69% from the spectrum is represented below of this number, and 18.7% from the distribution is recorded in 3-4 interval (excluded 0-1). While the distribution is slid toward high value portion (Fig3-b) such that 41% from the spectrum is represented below 5m/sec, and 10.7% from the distribution is recorded in 3-4 interval (excluded 0-1). Weibull probability density function representation of the histogram are shown in red curves in Fig.3. These two shapes will form the basis for the subsequent calculations.

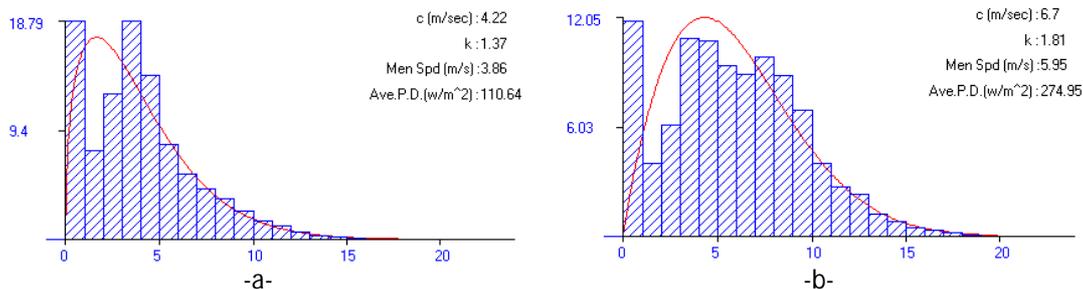
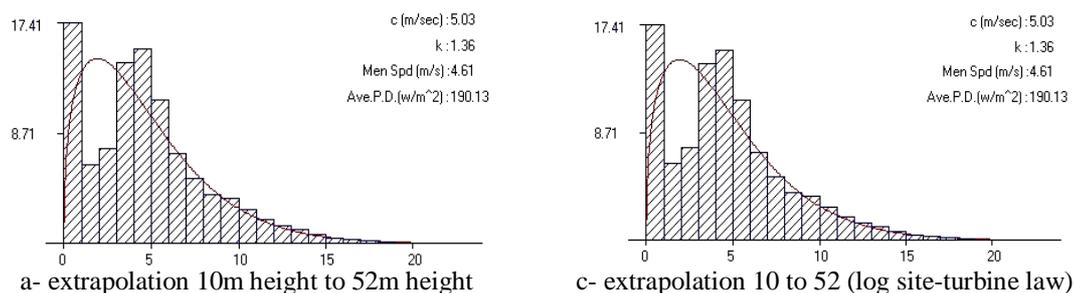


Fig. 3 Histogram and Weibull distribution for Al-Shehabi site at (a) 10m and (b) 52m height

The Power law and the Logarithmic law are the two most commonly used analytical models for extrapolating wind speeds to higher heights. The results of these two laws are shown in Figs. 4 and 5. Fig.4 represents the extrapolation of wind speed data using Logarithmic law, 1<sup>st</sup> column in this figure is founded using Eq.2, while 2<sup>nd</sup> column is founded using Eq.3. Fig4.a and Fig4.c represent the extrapolation from 10m to 52m height, Fig4.b and Fig4.d represent the extrapolation from 52m to 100m height. Weibull probability density function is plotted as continues red curves for the purpose of data representation.

Fig.5 represents the results of extrapolation using Power law, left column represents extrapolation from 10m height to 52m, whereas right column represents extrapolation from 52m height to 100m height at different wind shear exponent (Alpha) values 0.14, 0.2, and 0.25. These values have been selected on the basis that the standard is 0.14 and 0.25 value calculated from equation 5, while 0.2 value has been selected arbitrarily and as a value lies between two previous values.



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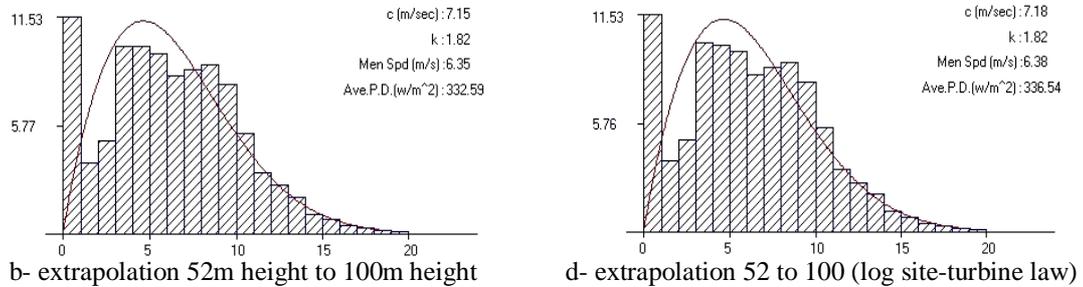


Fig. 4 Extrapolation using Logarithmic Law, 1st row represents extrapolation from 10m height to 52m height, 2nd row represents extrapolation from 52m height to 100m height

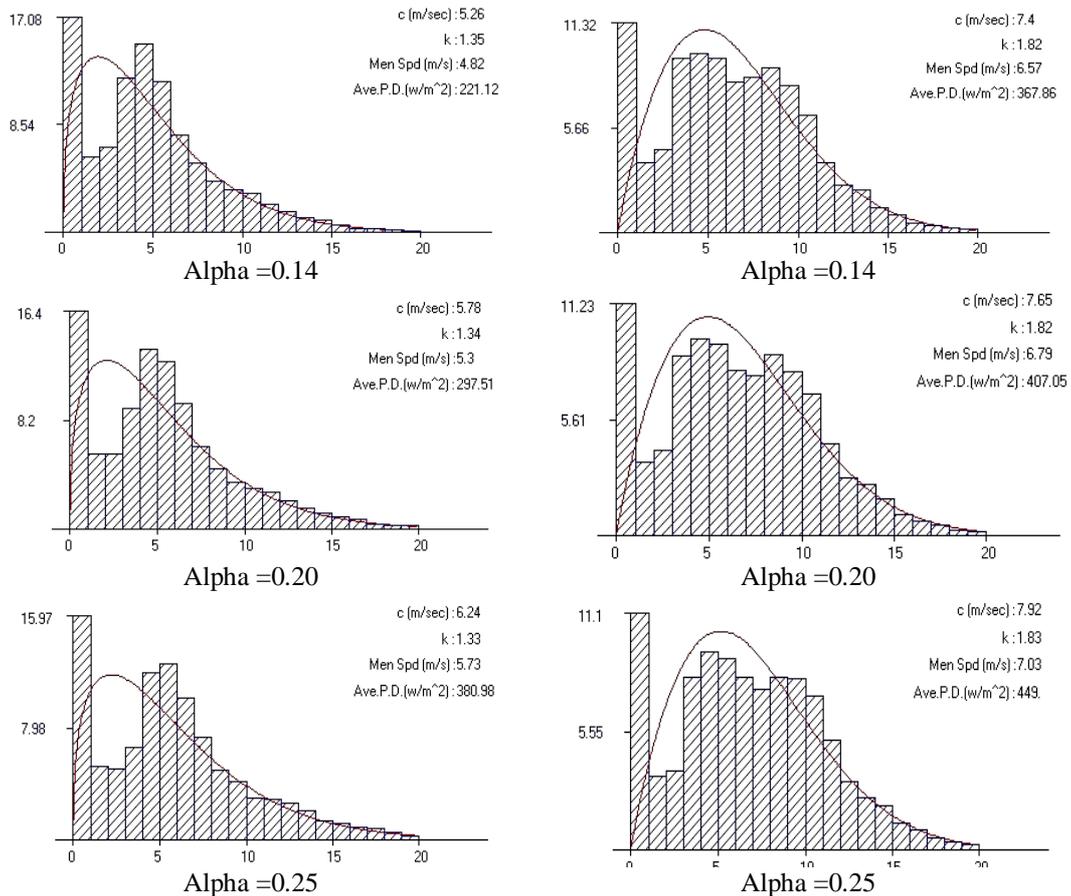


Fig. 5 Extrapolation using Power Law, left column represents extrapolation from 10m height to 52m height, right column represent extrapolation from 52m height to 100m height

The results derived from Figs. 3, 4, and 5 can be collected in the Table2 shown below.

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Table 2: Results Summary extrapolation of wind speed from 10 to 52 and from 52 to 100

ExtrapolationMethod	Geosun	Log(site-turbine) law (z0=0.0024)	Log law (z0=0.0024)	Power law (alpha=0.14)	Power law (alpha=0.2)	Power law (alpha=0.25) Using Eq. 5	Actual from tower at52m
Avg. wind speed at 52m	5.2 m/s	4.61 m/s	4.61 m/s	4.82 m/s	5.3 m/s	5.7 m/s	5.95m/s
P.D. at 52m	246 w/m <sup>2</sup>	190 w/m <sup>2</sup>	190 w/m <sup>2</sup>	221 w/m <sup>2</sup>	297 w/m <sup>2</sup>	380 w/m <sup>2</sup>	274w/m <sup>2</sup>
C at 52m	6.61 m/s	5.03 m/s	5.03 m/s	5.26 m/s	5.78 m/s	6.24 m/s	6.7m/s
K at 52m	1.80	1.36	1.36	1.35	1.34	1.33	1.81

Now, by applying equations 6 and 7 the wind speed distribution could be rise from 10m to 52m, the results is summarized in Table 3 below.

Table 3: Results of Weibull distribution extrapolation

	Actual at 52m	Extrapolated values 10m to 52m	Extrapolated values 10m to 100m	Geosun 100m
C(m/s)at 52m	6.7 m/s	6.3 m/s	7.38 m/s	7.30
K at 52m	1.81	1.6	1.71	1.73
Mean wind speed (m/s)	5.9	5.6	6.6	6.5
Power density (W/m <sup>2</sup> )	274.9	274	397	354

The 2<sup>st</sup> column in Table 2 gives the data taken from Geosun map; 3<sup>th</sup> and 4<sup>th</sup> columns show the extrapolated wind data from 10m height to 52m height by applying Logarithmic law (Eq.2) at roughness length equal to 0.0024. While 5<sup>nd</sup>, 6<sup>rd</sup>, and 7<sup>th</sup> columns in Table 2 give the extrapolated wind data from 10m height to 52m height by applying Power law (Eq.4) at alpha equal to 0.14, 0.2, and 0.25 respectively.

From Table 2 it can be concluded that the Power law gives better results than logarithmic law. This can be seen throughout the comparison between the wind speed and power density values that observed at a 52m height (taken from meteorological tower located at Al-Shehabi site) and data that calculated from Power law in order to extrapolate mean wind speed and power density from 10m to 52m height. The minimum difference between actual wind speed at 52m (5.95 m/s) and calculated one (5.7 m/s) is noticed at alpha equal to 0.25, while the minimum difference between actual power density at 52m (274 w/m<sup>2</sup>) and calculated one (297 w/m<sup>2</sup>) is noticed at alpha equal to 0.2.

Now, by a comparison between the above results of mean wind speed (5.95 m/s) and power density (274 w/m<sup>2</sup>) with the results exist in Table3 (mean wind speed 5.6 and power density 274 w/m<sup>2</sup>), it could infer that the distribution extrapolation gives more suitable results than that by using Power and Logarithmic laws.

From Fig.6 it could be easily seen the extent of convergence between the observed data (field data) and the results extracted from the process of probability distribution extrapolation.

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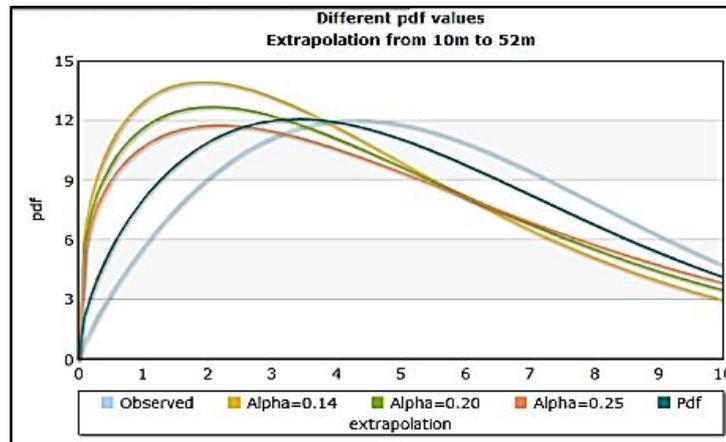


Fig.6 Comparison between all previous results, Pdf extrapolation is better way

## VIII. CONCLUSION

From the above discussion it could be concluded that:-

- 1- In case of data availability at a certain height and not available at a higher altitude than the previous, it is possible to use the extrapolation of wind speed or using the extrapolation of probability distribution.
- 2- It is possible to make wind speed extrapolation by mathematical laws such as Power law or Logarithmic law.
- 3- Power law gives more adequate results than logarithmic law.
- 4- Wind shear exponent (Alpha) is very important parameter in determining the accuracy of extrapolation. In another hand the determining of Alpha value by mathematical equation gives closer value to reality than the standard values.
- 5- The power law is widely used due to its simplicity, and it seems to give a better fit to most of the data over a greater height range and for higher wind conditions, compared to the log logarithmic law.
- 6- The results indicated that the process of distribution extrapolation gives more better results and more accurate than the using of mathematical laws.

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