Study of Various Downlink Systems with Multi Antenna Users

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ABSTRACT: The multiplexing gain for many users in downlink multi-antenna transmission system is only limited by the number of transmit antennas N and use of these antennas. In this paper we try to answer the question if the N data streams should be divided among few users (many streams per user) or many users (few streams per user, enabling receive combining). The prime work done in this paper is comparing the two SDMA strategies i.e ZFC (receive combining) and BD (multi-stream multiplexing). While contradicting observations on this topic have been reported in prior works, we show that selecting many users and allocating one stream per user (i.e., exploiting receive combining) is the best candidate under realistic conditions. This is explained by simulating results for Average Sum Rate and BER parameter. We also show that use of DFE method over MMSE method produces much better results, reducing the BER and increase the data rate. This fundamental result has positive implications for the design of downlink systems as it reduces the hardware requirements at the user devices and simplifies the throughput optimization.

KEYWORDS: Block-diagonalization, Decision feedback equalizer, MMSE algorithm, multi-user MIMO, zero forcing

INTRODUCTION

Wireless communication has been the subject of interest and active research over the past two decades. The performance of downlink wireless communication systems can be improved by multi-antenna techniques, which enable efficient utilization of spatial dimensions. In this paper we assume N is the number of base station antennas, and each user has M ≥ 1 antennas. Fortunately, the maximal multiplexing gain of N can be achieved by linear spatial division multiple access (SDMA) strategies [1], such as block-diagonalization (BD) [2], [3] and zero-forcing with combining (ZFC) [4], [5]. Such SDMA strategies transmit N simultaneous data streams, but can divide them among the users in different ways; the system can select between [N/M] and N users to be active and allocate from 1 to M streams to each of them. This raises a fundamental design question: how should the receive antennas at each user be used to maximize the system throughput?

Inter-user interference degrades user performance, while the mutual interference between users’ own streams can be handled by receive processing. It thus seems beneficial to only have a few active users and multiplex many streams to each of them. However, every additional stream allocated to a user experiences a weaker channel gain than the previous streams. If fewer than streams are allocated to a user, this user has degrees of freedom for interference-aware receive combining to achieve a strong effective channel and better spatial co-user compatibility. In other words, it is not clear whether receive antennas should be utilized for multi-stream multiplexing or receive combining. In this paper we try to find answer to the above statement. Spatial multiplexing system are studied based on two precoding techniques. We focus on the two SDMA strategies, namely zero forcing combing and block diagonalization. In this paper we see how stream allocation to users effects average sum rate and bit error rate parameter. The system performance with these parameters serve performance bound for precoded spatial multiplexing systems with minimum mean square error (MMSE) and decision feedback equalizer (DFE) applied receivers separately. This benchmark performance is not available before.
The authors of [5] claim that transmitting at most one stream per user is desirable when there are many users in the system. They justify this statement by using asymptotic results from [6] having many users. This argumentation ignores some important issues: 1) asymptotic optimality can also be proven with multiple streams per user; 2) the performance at practical values on K is unknown; and 3) the analysis implies an unbounded asymptotic multi-user diversity gain, which is a modelling artefact of fading channels [7]. Low-complexity algorithms have been proposed in [8]-[11], among others, by successively allocating data streams to users in a greedy manner. Simulations have indicated that fewer than N streams should be used when SNR and users are small, and that spatial correlation makes it beneficial to divide the streams among many users. Simulations in [9] indicates that the probability of allocating more than one stream per user is small when users grows large, but [9] only considers users with homogeneous channel conditions. Despite the similar terminology, our problem is fundamentally different from the classic works on the diversity-spatial multiplexing tradeoff (DMT) in [12], [13]. The DMT brings insight on how many streams should be transmitted in the high-SNR regime, while we consider how a fixed number of streams should be divided among the users. The authors of [3], [4] arrive at a different conclusion when they compare BD and ZFC under quantized CSI. Their simulations reveal a distinct advantage of BD (i.e., multi-stream multiplexing), but are limited to uncorrelated channels and neither include user selection nor interference rejection. We show that their results are misleading, because single-user transmission greatly outperforms both BD and ZFC in the scenario that they simulate. The author of [14] have used MMSE equalizer method at the receiver to show ZFC is better than BD by considering the average sum rate parameter. In this paper we show enhanced results for average rate parameter in addition to the reduction of error rate by applying DFEnonlinear equalization method at the receiver.

### III. PROPOSED METHODOLOGY

The use of multiple antennas at base stations and user devices is a key component in the design of cellular communication systems that can meet the capacity demands of tomorrow. Without affecting the multiplexing gain and for any given number of data streams, the system has the choice between allocating these streams to many users or few users. This tradeoff is investigated in this paper. The analysis is based on ZFC and BD precoding techniques, which represent the two extremes. ZFC only sends one data stream per scheduled user, thus each user can combine the received signals on its antennas to achieve receive diversity and interference rejection (i.e., an effective channel with better properties). BD selects fewer users than ZFC but multiplexes M streams to each of them, which relieves the interference mitigation and enables joint/iterative detection of each user’s streams. In other words, ZFC exploits receive combining and BD exploits multistream multiplexing.

Basically ZFC selects N users and sends N streams per user where as BD selects N/M users and sends M streams per user. Fig 1&2 shows two ways of dividing four data streams among multi-antenna users, which also represents two ways of utilizing the receive antennas to reduce interference. Fig 1 receives one stream per user and linearly combine the antenna to achieve an effective channel that rejects interference. Fig 2 receives multiple streams and handle their mutual interference through receive processing. Numerical simulations show that allocating one stream per active user is essentially optimal under realistic system conditions, and proves performance of ZFC outperforms BD. In this paper, we demonstrate the performance of 2 users for the multi user MIMO system. The scheme have been evaluated with 2 antennas at the transmitter side and 2 antennas at the receiver side for the ZFC precoding method and we allocate 1 stream per user in this method. Whereas for the BD precoding technique we consider 2 transmitter antennas and 4 antennas on the receiver side, thereby we multiplex 2 streams per user. Rayleigh channel is considered to be the channel model for analysing different precoding methods used for the transmission of MIMO signal the multi user environment. Rayleigh channel is used when there is no direct path between transmitter and receiver and the signal is subjected to many obstacles.
In wireless communications, channel state information (CSI) refers to known channel properties of a communication link. This information describes how a signal propagates from the transmitter to the receiver and represents the combined effect of scattering, fading, and power decay with distance. CSI needs to be estimated at the receiver and usually quantized and fed back to the transmitter. The CSI makes it possible to adapt transmissions to current channel conditions, which is crucial for achieving reliable communication with high data rates in multi-antenna systems. There are four major threats in the process of digital communication: namely, inter symbol interference (ISI), multipath propagation, co-channel interference, and presence of noise in the channel. Inter symbol interference arises when the data transmitted through the channel is dispersive, in which each received pulse is affected by adjacent pulses and due to which interference occurs in the transmitted signals. It is difficult to recover original data from one channel sample. Co-channel interference occurs in communication systems due to multiple access techniques using space, frequency or time. Multipath interference between consequently transmitted signals will take place if one signal is received whilst the previous signal is still being detected. In this paper, we try to resolve these issues with the help of an equalizer. It is located at the receiver end of the channel. Equalization is the process of adjusting the balance between the frequency components. It is used to mitigate the effects of ISI, Co-channel interference and noise that occurred in the signal from input to output. There are two types of equalizer called linear equalizer and nonlinear equalizer. In linear equalizer the output signal is not used in the feedback path to adapt the equalizer. The current and the past values of the received signal are linearly weighted by equalizer coefficients and summed to produce the output. In nonlinear equalizer the output signal is fed back to change the subsequent output of the equalizer. These structures have the flexibility to use various kinds of algorithms to quickly update the weights. Minimum mean square error (MMSE) is one of the types of linear equalizer used in the existing conventional scheme. In the proposed work, we use a type of nonlinear equalizer called Decision feedback equalizer (DFE) and compare the BER and average sum rate performance and for each of them using least mean square algorithm. The simulation results show that use of DFE scheme performs better than MMSE for the multi-user MIMO system.
IV. SIMULATIONS AND DISCUSSIONS

The outcomes are acquired by simulating the code in MATLAB. In this section we evaluate through simulations the performance of average sum rate and bit error rate. The bit error ratio is the number of bit errors divided by the total number of transferred bits during a studied time interval. Average sum rate is the system throughput or sum of the data rates that are delivered to all terminals in a network. Understanding the performance measure of BER and average sum rate parameter is very significant in better design of multi user MIMO system.

Fig. 3 BER compared with No:of data bits using BD-MMSE scheme

Fig 3 depicts the simulation using BD precoding MMSE technique for user1 and user2. The BER for user1 and user2 is observed to be $10^{-24}$ against the No:of data bits from 1 to 100. As we have already discussed ZFC precoding outperforms the BD precoding method, we can see from the below diagram how BER is reduced.

Fig. 4 BER compared with No:of data bits using ZFC-MMSE scheme

The above figure shows the simulation using ZFC precoding MMSE technique for user1 and user2. The BER for user1 and user2 is observed to be $10^{-26}$ and $10^{-29}$ respectively. When compared to the fig 3, one can find a significant reduction in BER. The error rate can be reduced further after application of nonlinear equalizer method namely Decision feedback equalizer which is contrary to the linear equalizer method called MMSE applied in the fig 3 and
Fig 4.

![Graph showing BER vs No: of data bits using BD-DFE technique]

**Fig. 5** BER compared with No: of data bits using BD-DFE technique

Fig 5 shows the simulation of BD with DFE method for user1 and user2 having BER value of $10^{-4}$ and $10^{-8}$ respectively which when compared with fig 3 shows reducing of error rate level.

![Graph showing BER vs No: of data bits using ZFC-DFE technique]

**Fig. 6** BER compared with No: of data bits using ZFC-DFE technique

Fig 6 shows BER value of user1 and user2 as $10^{-4}$ against the No: of data bits from 1 to 100. From the above simulation figures, it can be depicted that application of DFE (nonlinear equalizer method) technique at the receiver side reduces the error rate to a level which is lower what can be achieved using MMSE technique (linear equalizer method).

After analyzing the simulation results for BER, we shall now see how the average sum rate parameter varies against the No: of users, after the application of MMSE and DFE techniques separately.
Fig. 7: Average sum rate compared against No: of users using MMSE technique.

Fig 7 shows the simulation of average sum rate against the number of users. From the graph it can be depicted that as the number of users are increased, the average sum rate is also increased for users using ZFC and BD precoding methods using MMSE technique at the receiver side. Further it can also be seen that users using ZF precoding have greater sum rate compared to the user using BD precoding method, as explained in previous discussion.

Fig. 8: Average sum rate compared against No: of users using DFE technique

Fig 8 shows the simulation of average sum rate against number of users. This simulation result when compared to Fig 7 shows that users have greater increase in average sum rate with the implementation of DFE at the receiver side.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>BD-MMSE</th>
<th>ZFC-MMSE</th>
<th>BD-DFE</th>
<th>ZFC-DFE</th>
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<tbody>
<tr>
<td>BER-User1</td>
<td>$10^{-24}$</td>
<td>$10^{-28}$</td>
<td>$10^{-24}$</td>
<td>$10^{-3.95}$</td>
</tr>
<tr>
<td>BER-User2</td>
<td>$10^{-24}$</td>
<td>$10^{-29}$</td>
<td>$10^{-28}$</td>
<td>$10^{-3.95}$</td>
</tr>
<tr>
<td>Average sum rate-User1(bps)</td>
<td>18</td>
<td>32</td>
<td>21</td>
<td>39</td>
</tr>
<tr>
<td>Average sum rate-User2(bps)</td>
<td>13</td>
<td>28</td>
<td>19</td>
<td>39</td>
</tr>
</tbody>
</table>

Table 1: Comparison of simulation results
Table 1 tabulates the results from all the simulations discussed above. The simulation results when compared against each other reveal that Zero forcing combining precoding method is better than Block diagonalization precoding scheme. Further the implementation of a type of nonlinear equalization method called Decision feedback equalizer (DFE) at the receiver side reduces the Bit error rate (BER) and enhances the average sum rate with the increase in number of users. This simulation is quite better than the implementation of a type of linear equalization method called Minimum mean square error estimator (MMSE) technique for users using ZFC and BD precoding method.

V. CONCLUSION

This paper analysed how to divide data streams among users in a downlink system with many multi-antenna users; should few users be allocated many streams, or many users be allocated few streams? New and generalized analytic results were obtained to study this tradeoff. The main conclusion is that sending one stream per selected user and exploiting receive combining is the best choice under realistic conditions i.e. ZFC precoding method is better than BD precoding scheme. This is good as it reduces the hardware requirements at the users, compared with multi-stream multiplexing, and enables computationally efficient resource allocation. Further we have simulated the results for BER and Average sum rate parameter using Linear Equalizer method (MMSE) and Non Linear Equalizer method (DFE) separately. Comprehensive analysis of simulations reveal that implementation of DFE method reduces the error rate and enhances the average sum rate in comparison to the implementation of MMSE method at the receiver side.

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